

DIRICHLET BOUNDARY VALUE PROBLEM FOR A SYSTEM OF N THE SECOND ORDER ASYMPTOTICALLY ASYMMETRIC DIFFERENTIAL EQUATIONS

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We consider systems of the form

$$\begin{cases} x_1'' + g_1(x_1) = h_1(x_1, x_2, \dots, x_n), \\ x_2'' + g_2(x_2) = h_2(x_1, x_2, \dots, x_n), \\ \dots \\ x_n'' + g_n(x_n) = h_n(x_1, x_2, \dots, x_n) \end{cases}$$

along with the boundary conditions

$$x_1(0) = x_2(0) = \dots = x_n(0) = 0 = x_1(1) = x_2(1) = \dots = x_n(1)$$

provided that continuous right sides $h_i(x_1, x_2, \dots, x_n)$ ($i = 1, 2, \dots, n$) are bounded and satisfy the conditions $h_i(0, 0, \dots, 0) = 0$ ($i = 1, 2, \dots, n$). We suppose that $g_i(x_i)$ ($i = 1, 2, \dots, n$) asymmetric asymptotically linear functions, therefore at infinity the left sides behave like Fučík equations. We provide the existence results using the vector field rotation theory.

REFERENCES

- [1] A. Kufner and S. Fučík. *Nonlinear Differential Equations*. Elsevier, Amsterdam-Oxford-New York, 1980.
- [2] P.P. Zabrejko. Rotation of vector fields: definition, basic properties, and calculation. In: *Progress in Nonlinear Differential Equations and Their Applications*, v. 27, (Eds: M. Matzeu, A. Vignoli), Birkhäuser, Boston-Basel-Berlin, 1997, 445–601.
- [3] I. Yermachenko and F. Sadyrbaev. On a problem for a system of two the second order differential equations via the theory of vector fields. *Nonlinear Analysis. Modelling and Control*, **20** (2):175–189, 2015.